Critical slowing down as early warning for the onset and termination of depression

Ingrid A. van de Leemput[a,1,2], Marieke Wichers[b,1], Angélique O. J. Cramer[c], Denny Borsboom[c], Francis Tuerlinckx[d], Peter Kuppens[d,e], Egbert H. van Nes[a], Wolfgang Viechtbauer[b], Erik J. Giltay[f], Steven H. Aggen[g], Catherine Derom[h,i], Nele Jacobs[b,j], Kenneth S. Kendler[g,k], Han L. J. van der Maas[c], Michael C. Neale[g], Frenk Peeters[b], Evert Thiery[l], Peter Zachar[m], and Marten Scheffer[a]

[a]Aquatic Ecology and Water Quality Management, Wageningen University, 6700 AA, Wageningen, The Netherlands; [b]Department of Psychiatry and Psychology, School for Mental Health and Neuroscience, Maastricht University, 6200 MD, Maastricht, The Netherlands; [c]Department of Psychology, Psychological Methods, University of Amsterdam, 1018 XA, Amsterdam, The Netherlands; [d]Faculty of Psychology and Educational Sciences, KU Leuven–University of Leuven, 3000 Leuven, Belgium; [e]Melbourne School of Psychological Sciences, University of Melbourne, Melbourne, VIC 3010, Australia; [f]Department of Psychiatry, Leiden University Medical Center, 2300 RC, Leiden, The Netherlands; [g]Virginia Institute for Psychiatric and Behavioral Genetics and Department of Psychiatry, Virginia Commonwealth University, Richmond, VA 23298; [h]Centre of Human Genetics, University Hospitals Leuven, and [i]Department of Human Genetics, KU Leuven, 3000 Leuven, Belgium; [j]Department of Psychology, Open University of The Netherlands, 6401 DL, Heerlen, The Netherlands; [k]Department of Human and Molecular Genetics, Medical College of Virginia, Virginia Commonwealth University, Richmond, VA 23298; [l]Department of Neurology, Ghent University Hospital, Ghent University, 9000 Ghent, Belgium; and [m]Department of Psychology, Auburn University Montgomery, Montgomery, AL 36117

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About 17% of humanity goes through an episode of major depression at some point in their lifetime. Despite the enormous societal costs of this incapacitating disorder, it is largely unknown how the likelihood of falling into a depressive episode can be assessed. Here, we show for a large group of healthy individuals and patients that the probability of an upcoming shift between a depressed and a normal state is related to elevated temporal autocorrelation, variance, and correlation between emotions in fluctuations of autorecorded emotions. These are indicators of the general phenomenon of critical slowing down, which is expected to occur when a system approaches a tipping point. Our results support the hypothesis that mood may have alternative stable states separated by tipping points, and suggest an approach for assessing the likelihood of transitions into and out of depression.

early warning signals | experience sampling method | critical transitions | positive feedback

Depression is one of the main mental health hazards of our time. It can be viewed as a continuum with an absence of depressive symptoms at the low endpoint and severe and debilitating complaints at the high end (1). (Throughout this manuscript, the term "depression" refers to this continuum of depressive symptoms.) The diagnosis major depressive disorder (MDD) defines individuals at the high end of this continuum. Approximately 10–20% (2) of the general population will experience at least one episode of MDD during their lives, but even subclinical levels of depression may considerably reduce quality of life and work productivity (3). Depressive symptoms are therefore associated with substantial personal and societal costs (4, 5). The onset of MDD in an individual can be quite abrupt, and similarly rapid shifts from depression into a remitted state, so-called sudden gains, are common (6). However, despite the high prevalence and associated societal costs of depression, we have little insight into how such critical transitions from health to depression (and vice versa) in individuals might be foreseen. Traditionally, the broad array of correlated symptoms found in depressed people (e.g., depressed mood, insomnia, fatigue, concentration problems, loss of interest, suicidal ideation, etc.) was thought to stem from some common cause, much as a lung tumor is the common cause of symptoms such as shortness of breath, chest pain, and coughing up blood. Recently, however, this common-cause view has been challenged (7–9). The alternative view is that the correlated symptoms should be regarded as the result of interactions of components of a complex dynamical system (7, 10–12). Consequently, new models of the etiology of depression involve a network of interactions between components, such as emotions, cognitions, and behaviors (8, 9). This implies, for instance, that a person may become depressed through a causal chain of feelings and experiences, such as the following: stress → negative emotions → sleep problems → anhedonia (9, 13–15). However, the network view also implies that there can be positive feedback mechanisms between symptoms, such as the following: worrying → feeling down → more worrying or feeling down → engaging less in social life → feeling more down (16). It is easy to imagine that such vicious circles could cause a person to become trapped in a depressed state.

The plausibility of this theoretical framework with regard to MDD is supported in at least four ways. First, intraindividual analyses of multivariate time series of variables related to MDD symptomatology show clear interactions between these variables (15–17). Second, MDD symptoms display distinct responses to different life events (18, 19) and are differently related to other external variables and disorders (20), which is consistent with a network view of interacting variables related to MDD

Significance

As complex systems such as the climate or ecosystems approach a tipping point, their dynamics tend to become dominated by a phenomenon known as critical slowing down. Using time series of autorecorded mood, we show that indicators of slowing down are also predictive of future transitions in depression. Specifically, in persons who are more likely to have a future transition, mood dynamics are slower and different aspects of mood are more correlated. This supports the view that the mood system may have tipping points where reinforcing feedbacks among a web of symptoms can propagate a person into a disorder. Our findings suggest the possibility of early warning systems for psychiatric disorders, using smartphone-based mood monitoring.

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[1]I.A.v.d.L. and M.W. contributed equally to this work.

[2]To whom correspondence should be addressed. E-mail: ingrid.vandeleemput@wur.nl.

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symptomatology, but not with a classical disease model that postulates the existence of a common cause (21). Third, when asked how MDD symptoms are related, clinical experts report a dense set of causal relations between them (9, 22). Fourth, using recently developed self-report methods, it has been shown that individuals with elevated symptom levels typically report causal interactions between their symptoms, including those of MDD (23, 24).

Thus, there is ample evidence to support the thesis that MDD is characterized by causal interactions between its "symptoms." From dynamical systems theory, it is known that positive-feedback loops among such causal interactions can cause a system to have alternative stable states (25). This has profound implications for the way a system responds to change. For example, gradually changing external conditions may cause a system to approach a tipping point. Close to such a point, the system typically loses resilience, that is, increasingly small perturbations may suffice to cause a shift to an alternative stable state (25). In the mood system, characterized by the "mood state" of an individual that may range from normal to severe depression, stressful conditions may bring the system to such a fragile state (26). For example, a chronically unpleasant working situation may reduce resilience of the "normal state" by precipitating insomnia and other related symptoms. Then, only a slight additional perturbation (e.g., an unpleasant phone call with mother-in-law) may be enough to trigger a chain of symptoms that causes the system to shift from a stable normal state into an alternative "depressed state."

In this paper, we analyze time series of four emotions as the observed variables of the mood system in healthy persons and depressed patients providing support for the view that the mood system can have tipping points. Specifically, we show indicators of critical slowing down (27), which have recently been shown to be linked to tipping points in a range of complex systems (28–30). These indicators can be used as early warning signals that can help assess the likelihood that an individual will go through a major transition in mood. Before moving to the empirical evidence, we briefly introduce the generic phenomenon of critical slowing down, using a simple model of the mood system as an illustration.

Results and Discussion

Theory of Critical Slowing Down. Marked transitions from one dynamical regime to a contrasting one are observed in complex systems ranging from oceans, the climate, and lake ecosystems, to financial markets. Such "regime shifts" (31) can simply be the result of a massive external shock, or stepwise change in the conditions. However, it is also possible that a slight perturbation can invoke a massive shift to a contrasting and lasting state. It is intuitively clear that this can happen to an object such as a chair or a ship when it is close to a tipping point, but complex systems such as the climate or ecosystems can also have tipping points (25). The term tipping point in such systems is informally used to refer to a family of catastrophic bifurcations in mathematical models (32), which in turn are simplifications of what characterizes the stability properties of real complex systems (25).

As tipping points can have large consequences, there is much interest in finding ways to know whether a catastrophic bifurcation is near. In principle, this could be computed if one has a reliable mechanistic model. However, we have little hope of having sufficiently accurate models for complex systems such as lakes or the climate, let alone psychiatric disorders. A recent alternative approach is to look for indicators of the proximity of tipping points that are generic in the sense that they do not depend on the particular mechanism that causes the tipping point. A possibility that has attracted much attention is that, across complex systems, the vicinity of a tipping point may be detected on the basis of a phenomenon known as "critical slowing down" (32, 33). Specifically, critical slowing down happens as the dominant eigenvalue, characterizing the return rate to equilibrium upon small perturbations, goes to zero in tipping points related to zero-eigenvalue bifurcations. On an intuitive level, this can be understood from a ball-in-a-cup diagram (Fig. 1 *A* and *B*). As the slope represents the rate of change, close to the tipping point where the basin of attraction becomes shallower, return to equilibrium upon

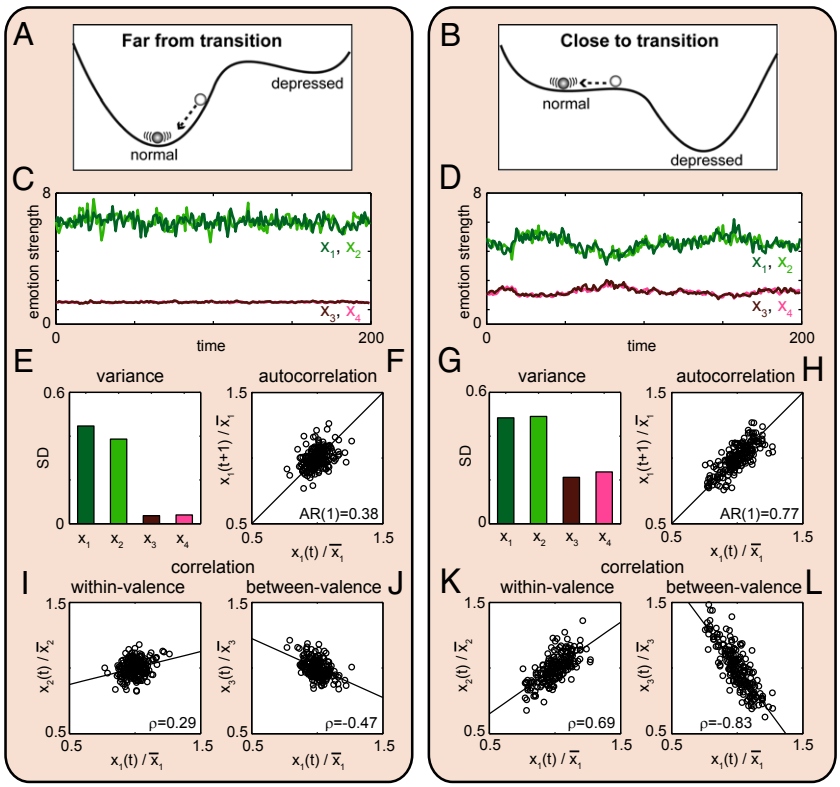

Fig. 1. Model simulations illustrating generic indicators of proximity to a tipping point from a normal to a depressed state. The stability of a healthy person may become more fragile close to a transition toward depression, which can intuitively be understood from a ball-in-a-cup diagram (*B* versus *A*). This fragility would lead to critical slowing down in a system with tipping points between alternative stable states, illustrated by model simulations. Under a permanent regime of stochastic perturbations on the strength of each emotion (*C* and *D*), slowing down near the tipping point results in higher variance (SD = standard deviation) in emotion strength (*G* versus *E*), higher temporal autocorrelation [AR(1) = lag-1 autoregression coefficient] in emotion strength (*H* versus *F*), and stronger correlation (ρ = Pearson correlation coefficient) between emotion strength of emotions with the same valence (*K* versus *I*), and between emotions with different valence (*L* versus *J*). Positive emotions are represented by x_1 and x_2, and negative emotions by x_3 and x_4. Parameters: (*Left*) $r_3 = r_4 = 0.5$, (*Right*) $r_3 = r_4 = 1.18$.

small perturbations will become slower. Although critical slowing down has been known for a long time in mathematics, slowing down at tipping points has only recently been demonstrated experimentally in living systems (34, 35).

For most systems, it is either impractical or unethical to experimentally perturb them to find out if they are close to a tipping point. However, any system, including mood, is continuously subject to small natural perturbations. One can imagine the effect as a combination of direct impacts on the ball (in models this corresponds to so-called additive noise) and fluctuations in the shape of the stability landscape (multiplicative noise). A range of modeling studies, laboratory experiments, and field studies now suggests that, under such stochastic conditions, critical slowing down typically causes an increase in the variance and temporal autocorrelation of fluctuations in the system elements (29, 30, 34–37). Besides, in a network of fluctuating elements, one expects an increase in cross-correlation between elements that will shift together (38). This implies the possibility that elevated variance and correlation may be used as indicators of critical slowing down and therefore as early warning signals that may reveal the loss of resilience in the proximity of a tipping point (27).

Minimal Models of Mood. Critical slowing down will occur independently of the specific mechanisms involved in bringing about a tipping point. However, to illustrate how indicators of critical slowing down might signal the proximity of a tipping point in mood, we use a simple dynamical model, based on the classical and well-studied Lotka–Volterra equations (*Materials and Methods*). This is about the simplest way of modeling positive and negative interactions between dynamically varying entities such as populations of organisms. Specifically, we model four emotions as variables of the mood system (reflecting the four quadrants of the affective circumplex: cheerful, content, sad, and anxious; see ref. 39), and assume that emotions with the same "valence" (positive or negative) promote each other, whereas emotions of opposite valence tend to compete (*SI Appendix*, Fig. S1*A*). This is of course an overly simple representation of the mood system, but consistent with the empirical observations that same-valenced emotions tend to augment and opposite-valenced emotions tend to blunt each other (16, 40), and that this dynamic interplay has relevance for the course of depression (41). Also on theoretical grounds, it stands to reason that emotions that show large overlap in terms of their underlying components (such as appraisals; see ref. 40) would augment each other, whereas emotions that diverge in these components, would counteract each other (40). Given suitable parameter settings, the model has two alternative stable states over a range of conditions: one state dominated by strong positive emotions, the normal state, and the second dominated by strong negative emotions, the depressed state (*SI Appendix*, Fig. S1*B*).

To mimic the stochastic environment, we expose the model to a regime of random perturbations (Fig. 1 *C* and *D*). The resulting fluctuations in the strength of the four modeled emotions show signs of critical slowing down as expected from the generic theory (27). Specifically, close to the tipping point toward depression, the fluctuations have a higher variance (Fig. 1 *G* versus *E*), and temporal autocorrelation (Fig. 1 *H* versus *F*). Also, the cross-correlations between the strength of the modeled emotions become stronger in the vicinity of the tipping point (Fig. 1 *K* and *L* versus *I* and *J*). Note that positive correlations between emotions within the same valence will tend toward 1 (Fig. 1*K*), whereas negative correlations between opposed valence emotions will tend toward −1 (Fig. 1*L*). Similarly, once the model system is in the depressed state, we see elevated variance and correlations close to the critical point of recovery (*SI Appendix*, Fig. S2).

Although the view of mood as consisting of interactions between its various components (e.g., cheerful and sad) fits well with recent theories regarding the pathology of MDD (7, 8), one could argue that such mood variables (unlike, for instance, populations of animals) are not on equal par with true physical quantities. Rather, emotions such as feeling cheerful or anxious seem to be the result of complex interactions between biology (including genetics), previous life experiences, and current contextual influences. We will probably never be able to assess and understand the full complexity of this system. However, psychologists work with emotions because they are thought to reflect meaningful aspects of the mood system (39, 42). In fact, the subjective experience component of emotions is thought to function as a monitoring tool for organisms to detect important changes in the complex mood system (39). Given that emotions are unitless subjective measures that are not governed by any laws of conservation, one could wonder if they should still be expected to reflect critical slowing down if that underlying system approaches a tipping point. To explore this, we made a model of a complex network of interactions between 20 variables, representing (in principle) objectively measurable components of mood (e.g., elements ranging from neurotransmitter and hormone concentrations to physical activity modes and social interactions). We created the model such that it has tipping points. Then, we mimicked the strength of emotions as indirect indicators of the state of the highly complex network by using principal components [principal component analysis (PCA) axes] (*SI Appendix*, *Text S1*). Analyses of this model illustrate that critical slowing down remains clearly reflected in the PCA-based indicators (*SI Appendix*, Figs. S3–S5 and *Text S1*).

Clearly, many other dynamical models of the mood system could be conceived. However, the examples we analyzed may serve to illustrate the general phenomenon that indicators of critical slowing down can be found at tipping points independently of the precise underlying complex mechanisms involved, and on the way the variables are measured (27, 28, 43). Thus, even if we cannot attain a complete understanding of the complex array of mechanisms that are involved in regulating mood, we may expect that, if transitions in mood are related to the proximity of tipping points, the likelihood of such shifts to happen should be evident in indicators of critical slowing down.

Patterns in Recorded Mood Dynamics. To explore whether mood dynamics do indeed display such indications of critical slowing down before tipping points in depression, we analyzed time series of four emotions (cheerful, content, sad, and anxious) as observed variables of the overall mood state obtained through the Experience Sampling Method (ESM) (*Materials and Methods*), in which subjects have monitored, for each emotion, their position on an emotional scale during 5–6 consecutive days. We refer to this as their "emotion score" at a certain time. We studied a general population sample that varies in the development of depressive symptoms over time (in follow-up measurements). Some subjects shifted upward along the continuum of depression and some downward. A fraction of this group (13.5%) showed a transition from a normal state to a DSM-IV clinical diagnosis of MDD. We investigated in this general population sample whether indicators of critical slowing down are associated with elevated risk of future shifts toward depression. In addition, we analyzed ESM data from a population sample of depressed patients to see whether critical slowing down is related to the probability of upcoming recovery (for sample descriptions, see *SI Appendix*, Table S1).

Both temporal autocorrelation (i.e., the autoregression coefficient) and variance of fluctuations in emotion scores were higher in individuals with upcoming transitions (Fig. 2 and *SI Appendix*, Tables S2 and S3). For an impending worsening of depressive symptoms, these signals are strongest for negative emotions (Fig. 2 *A* and *C*), whereas for an upcoming improvement in depressive symptoms in individuals with current MDD, these signals are strongest for positive emotions (Fig. 2 *B* and *D*) compared with the other emotions (*SI Appendix*, Fig. S6). Also, correlations between emotion scores were consistently stronger for individuals who experienced a future transition upward on the continuum of depression (Fig. 3 *A* and *C*) as well as in depressed patients who were moving downward on the continuum

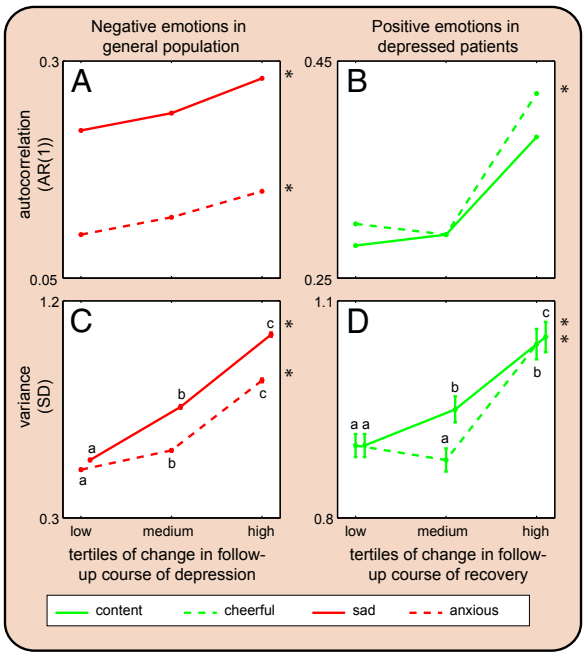

Fig. 2. Temporal autocorrelation and variance of emotion scores as a function of future symptoms. Increasing autocorrelation [AR(1) = mean lag-1 autoregression coefficient] (*A* and *B*) and variance (SD = mean standard deviation) (*C* and *D*) of negative emotions according to tertiles of development of future depressive symptoms in a general population ($n = 535$) (*Left*), and of positive emotions according to tertiles of future recovery in depressed patients ($n = 93$) (*Right*). For temporal autocorrelation (*A* and *B*), we present data according to tertiles of change in follow-up course for illustrative purposes only; however, note that in the statistical analyses continuous variables were used. Asterisks indicate a significant upward trend in temporal autocorrelation (positive interaction effect of future symptoms: $P < 0.05$). For variance (*C* and *D*), error bars represent SEs. Note that the SEs in *C* are very small. Asterisks indicate an overall significant upward trend in variance (overall tests: $P < 0.05$). Mean values represented by different letters within emotions are significantly different (post hoc tests: $P < 0.05$).

within the study period (Fig. 3 *B* and *D*) (*SI Appendix*, Table S4). Note that the main structure of our model of positive and negative interactions is consistent with the data: emotions of opposite valence affect each other negatively, whereas emotions with the same valence are positively correlated (Fig. 3).

The rise in temporal correlations and cross-correlations is likely a more direct indicator than the rise in variance. This is because change in variance can be confounded by several mechanisms (44). For instance, a trend in variance may be related to a trend in the mean. Indeed, such a coupling of variance to mean may partly explain the trends we observe in upcoming emotions (*SI Appendix*, Fig. S6). However, an analysis of trends in the coefficients of variation illustrates that, especially in the general population, rising variability in all emotions may be an observable indicator of critical slowing down associated with an elevated risk of an impending depression (*SI Appendix*, Fig. S7). Also, one could argue that the observed effect in variance might be an effect of increased external perturbations ("noise" in the model), and not a result of critical slowing down. As temporal autocorrelation and cross-correlations are independent of the means as well as the amplitude of noise (44), the trends in correlations may be our most robust indicator of critical slowing down.

Taken together, our results suggest that there is an elevated chance of upcoming shifts between a depressed and a normal mood state in persons who show indications of critical slowing down in their emotion scores. This is consistent with the idea that such transitions tend to happen when a subject is close to a tipping point. The relationship between elevated temporal correlations and upcoming transitions we detected is also consistent with independent earlier studies, showing that "emotional inertia" (slower rates of change in emotion scores) is associated with future transition into a more depressed state (45, 46). Moreover, the corresponding view of depression as an alternative stable state is in line with the finding of reinforcing feedbacks between emotions, and with the sudden character of shifts to depression and recovery (6).

Importantly, this body of evidence does not imply that all persons would have such tipping points. It seems more likely that whereas some persons abruptly shift between a normal and a depressed state, for others, certain positive-feedback mechanisms (e.g., feeling down → engaging less in social life → feeling more down) remain too weak to cause alternative stable states. Such persons would be expected to move more gradually between a normal and a depressed state, experiencing intermediate states to be stable as well. Indeed, dynamical systems with tipping points will often respond more smoothly if the positive feedback responsible for this feature becomes weaker (*SI Appendix*, Fig. S8). Hints of slowing down may still be detected for persons without alternative stable states in case their mood responds relatively strongly to a gradual change in conditions. This is because some slowing down (albeit not full-blown critical slowing down, where recovery rate upon perturbation reaches zero) is expected across a wide range of situations where systems respond relatively sensitively around a threshold (47).

Implications. Clearly, the effects of stressors may differ widely between persons and contexts depending on a complex set of interacting factors shaped by genes and history (e.g., genetic variants, epigenetic regulation, early life events, and connection strength between neurons that are changed by experience). This makes it unlikely that we would ever be able to obtain accurate

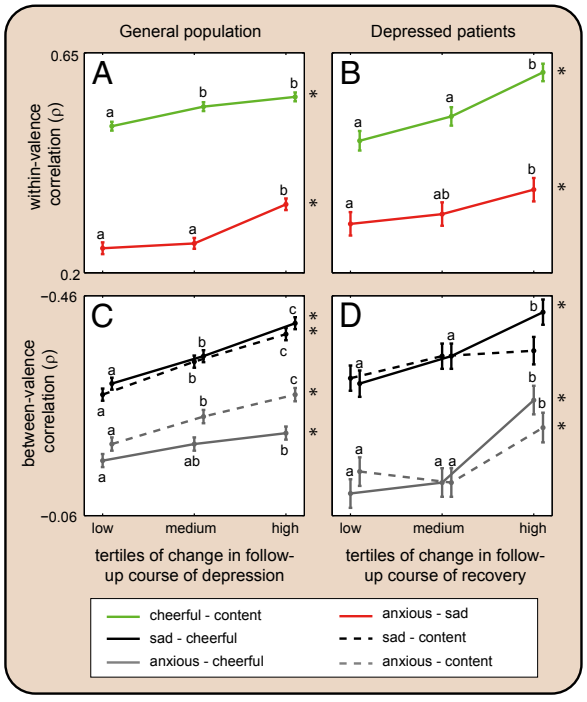

Fig. 3. Correlations between emotion scores as a function of future symptoms. Strengthening correlations between emotions of the same valence (*A* and *B*), and between emotions of different valence (*C* and *D*) according to tertiles of the development of future depressive symptoms in a general population ($n = 535$) (*Left*), and to tertiles of future recovery in depressed patients ($n = 93$) (*Right*). Error bars represent SEs. Asterisks indicate an overall significant strengthening trend in correlation (overall tests: $P < 0.05$). Mean values represented by different letters within emotions are significantly different (post hoc tests: $P < 0.05$).

individual predictions of risk for relapse or recovery based on a mechanistic insight into the mood regulation system. However, if the mood system, as our results suggest, shows signals of critical slowing down, we may use this generic feature to improve our ability to anticipate clinically relevant mood shifts, even in the absence of a full understanding of the complex underlying system that is responsible for such shifts. Clearly, such mechanistic insight may be important to develop better treatment strategies. However, when it comes to risk stratification, the indicators of critical slowing down may be a powerful and independent addition to our clinical toolkit.

This has important implications for treatment. Mood data suitable for analysis of critical slowing down are now easy to assess and monitor, for instance through an app on a smartphone. Furthermore, web applications are able to provide user-friendly feedback to patients and clinicians on the patient's critical slowing-down patterns. The ability to anticipate transitions (e.g., a shift upward on the continuum of depression for a person at risk, or a shift downward on the continuum for a patient with current MDD) could prove beneficial in terms of the timing and magnitude of treatment interventions. This information may prove especially valuable in optimizing health care and in reducing mental health care costs. Hence, in terms of understanding and treating psychiatric disorders like depression, the potential gains associated with our approach are considerable. Therefore, our central hypothesis—that symptomatology like depression should be conceptualized as alternative states of complex dynamical systems—is not an endpoint; rather, it should mark the beginning of novel research programs.

Materials and Methods

Samples. We analyzed data from (*i*) the general population (females; n = 621) and (*ii*) depressed patients eligible for treatment (n = 118; for sample descriptions, see *SI Appendix*, Table S1). The first sample was recruited from a population-based sample of the East-Flanders Prospective Twin Survey (Belgium). The data of depressed patients came from two studies. Both included baseline ESM measurements followed by an intervention (either a combination of pharmacotherapy and supportive counseling or allocation to either imipramine or placebo) and follow-up assessments of depressive symptoms. For details on inclusion criteria and final set of participants, see *SI Appendix, Text S2*. A total of 535 individuals from the general population and 93 depressed patients were included in the final analyses.

ESM. To calculate early warning signals for transition, the four emotions were measured repetitively and prospectively using the ESM. This structured diary technique prospectively assesses individual experience in the context of daily life (48, 49). Subjects received a digital wristwatch and a set of ESM self-assessment forms collated in a booklet for each day. The wristwatch was programmed to emit a signal ("beep") at an unpredictable moment in each of 10 90-min time blocks between 0730 hours and 2230 hours, on 5 or 6 consecutive days, depending on the study. After each beep, subjects were asked to fill out the ESM self-assessment forms, including emotion scores on seven-point Likert scales. This resulted in a maximum of 50 or 60 measurements, depending on the study. The local ethics committees of Maastricht and Leuven University granted permission and all participants had provided their informed consent.

Design. All participants underwent a baseline period of ESM. In the depressed patients, follow-up course of depression was measured with the Hamilton Depression Rating Scale (HDRS-17) at 6–8 wk following start of treatment. In the general population, the Symptom Checklist 90 (SCL-90-R) was completed at baseline and at four follow-up measurements, ∼3 mo apart from each other. Follow-up depression score was based on the average of the four follow-up measurements.

Analyses. The aim was to analyze whether the hypothesized early warning signals (autoregression coefficients, variance, and correlation between emotions as derived from the repeated ESM measures) are associated with follow-up course of depression in both samples. Analyses were performed for four emotions that were a priori chosen to represent each quadrant of the affective space defined by valence and arousal (39): feeling cheerful (positive valence, high arousal), content (positive valence, low arousal), anxious (negative valence, high arousal), and sad (negative valence, low arousal). Data on these four emotions were available in both samples. Because the ESM data have a hierarchical structure [in which the four emotions are clustered within measurement moments (about 50–60 "beeps") and measurement moments are clustered within persons], a statistical model needs to be used that deals appropriately with the hierarchical structure. These models are known as multilevel models. Two different models were used (see *Multilevel Model 1: Autocorrelation*). All multilevel models included modeling of random intercept and slope. Data were analyzed using STATA 12.1 (50) and most analyses were replicated independently in R (51). See *SI Appendix, Text S2* for details on heteroscedasticity and normality, and Dataset S1 for the R code.

Multilevel Model 1: Autocorrelation. To extract the information on autocorrelation, we analyzed each emotion separately. A multilevel model was set up in which the emotion score at time t (e.g., anxious at time t) is predicted by the emotion score at time $t-1$ (e.g., anxious at time $t-1$). The regression coefficient of the emotion scores at time $t-1$ on emotion scores at time t is the autoregression coefficient. In the model we used, we additionally included an interaction between the emotion scores at time $t-1$ and follow-up course of depression. This means that in this model the size of the autoregression coefficient for a person depends on the continuous follow-up course of depression score. Thus, the autoregression coefficient (and henceforth the autocorrelation) may differ between people with a different follow-up course of depression score. In this way, we are able to test whether persons whose depression score shows a large change over time, will have a higher autoregression coefficient, whereas persons whose depression score shows little change, will have a lower autoregression coefficient (this being the phenomenon of critical slowing down). However, the follow-up in course of depression score is probably not the only variable that is related to differences in autoregression coefficients between persons. A multitude of other variables may contribute to the individual differences in the autoregression coefficient. For this reason, a person-specific deviation is added to the regression coefficient of the person, which is drawn from a normal distribution with zero mean and a to-be-estimated variance, which makes the model formally a multilevel regression model. (Note that also the intercept of the regression model is assumed to be random.) In this way, we are able to examine the association between autoregression coefficients of the four emotions and follow-up course of depression. This multilevel approach enables us to assess this so-called interaction effect between emotion scores at time $t-1$ and the follow-up course of depression, while respecting the hierarchical structure of the data. Note that for the purpose of visualization tertiles of depression scores were used in Fig. 2 and *SI Appendix*, Fig. S6 (see *Multilevel Model 2: Variance and Correlations* for the definition of the tertile groups).

Multilevel Model 2: Variance and Correlations. In this second multilevel model, we examined the extent to which variance and correlations differ with follow-up course of depression. In contrast to the autocorrelation analysis, we first clustered the individuals into discrete tertile groups according to follow-up course of depression score and used these tertile groups in our analysis (instead of the continuous score). Those individuals in the general population with the lowest level of depressive symptoms (33%) at follow-up were classified as group 1, those in the middle (33%) as group 2, and the highest 33% as group 3. Similarly, patients with the lowest decrease in symptoms over course of treatment were classified as group 1, those in the middle as group 2, and those with the highest decrease as group 3. Ideally, we would have liked to model the variances and correlations in some (non)linear way as a function of the covariate (future depressive symptoms) in the context of a multilevel model directly, but appropriate models for such an analysis have not been fully developed and tested yet. In the analyses, all four emotions were simultaneously considered. This creates a three-level structure: emotions nested in measurement moments nested in persons. For each tertile group, a multilevel regression model was fitted with emotion score as the dependent variable and dummy codes for the four emotions as independent variables. Random effects corresponding to these dummy-coded variables were added at the person and at the measurement level. These random effects were allowed to have different variances for the four items and their correlations were estimated freely. Therefore, no structure was imposed on the model, making this a saturated model [i.e., the model with the most complex covariance structure possible for the data at hand (52)] The estimated variation in these random effects was used to estimate variance in emotion scores at the measurement level. Correlations between these random effects were used to estimate correlations between emotions at the measurement level. Wald-type tests were used to test for overall differences in the variances and correlations between the three groups.

The Dynamical Systems Model. We analyzed a minimal model, simulating interactions between four modeled emotions in a person as a stochastic differential equation (inspired by the Lotka–Volterra models, as in ref. 53):

$$\frac{dx_i}{dt} = (r_i + \epsilon_r)x_i + \sum_j^4 C_{i,j}x_j x_i + \mu,$$

where x_1 and x_2 signify the strength of positive emotions (such as cheerful and content), and x_3 and x_4, the strength of negative emotions (such as sad and anxious). The maximum rate of change of the positive emotions, r_1 and r_2, was set to 1, whereas the maximum rate of change of the negative emotions, r_3 and r_4, was assumed to be stress-related, ranging between 0.5 (low stress) and 1.5 (high stress). The matrix C represents the interaction network between the emotions:

$$C = \begin{pmatrix} -0.2 & 0.04 & -0.2 & -0.2 \\ 0.04 & -0.2 & -0.2 & -0.2 \\ -0.2 & -0.2 & -0.2 & 0.04 \\ -0.2 & -0.2 & 0.04 & -0.2 \end{pmatrix}$$

Each term of this interaction network describes the strength and direction of the interaction. Negative terms mean that these emotions suppress each other and positive terms imply enhancement. The maximum rate of change (r_i) of each emotion was subjected to a noise term (ϵ_r) representing short-term fluctuations in the rate of change of each emotion. ϵ_r is represented by a Gaussian white-noise process of mean zero and intensity σ^2/dt ($\sigma = 0.15$). Effectively, this means that the system is subject to multiplicative noise. Independent of the strength of the emotions, their value increases by a fixed amount ($\mu = 1$) to prevent emotion levels to be close to zero. The model was solved using a Euler–Maruyama scheme in MATLAB.

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1. Hankin BL, Fraley RC, Lahey BB, Waldman ID (2005) Is depression best viewed as a continuum or discrete category? A taxometric analysis of childhood and adolescent depression in a population-based sample. *J Abnorm Psychol* 114(1):96–110.
2. Bijl RV, Ravelli A, van Zessen G (1998) Prevalence of psychiatric disorder in the general population: Results of The Netherlands Mental Health Survey and Incidence Study (NEMESIS). *Soc Psychiatry Psychiatr Epidemiol* 33(12):587–595.
3. Rodríguez MR, Nuevo R, Chatterji S, Ayuso-Mateos JL (2012) Definitions and factors associated with subthreshold depressive conditions: A systematic review. *BMC Psychiatry* 12:181.
4. Kessler RC, et al. (1994) Lifetime and 12-month prevalence of DSM-III-R psychiatric disorders in the United States. Results from the National Comorbidity Survey. *Arch Gen Psychiatry* 51(1):8–19.
5. Lopez AD, Mathers CD, Ezzati M, Jamison DT, Murray CJL (2006) Global and regional burden of disease and risk factors, 2001: Systematic analysis of population health data. *Lancet* 367(9524):1747–1757.
6. Aderka IM, Nickerson A, Bøe HJ, Hofmann SG (2012) Sudden gains during psychological treatments of anxiety and depression: A meta-analysis. *J Consult Clin Psychol* 80(1):93–101.
7. Kendler KS, Zachar P, Craver C (2011) What kinds of things are psychiatric disorders? *Psychol Med* 41(6):1143–1150.
8. Cramer AOJ, Waldorp LJ, van der Maas HLJ, Borsboom D (2010) Comorbidity: A network perspective. *Behav Brain Sci* 33(2-3):137–150, discussion 150–193.
9. Borsboom D, Cramer AOJ (2013) Network analysis: An integrative approach to the structure of psychopathology. *Annu Rev Clin Psychol* 9:91–121.
10. Huber MT, Braun HA, Krieg JC (1999) Consequences of deterministic and random dynamics for the course of affective disorders. *Biol Psychiatry* 46(2):256–262.
11. Hayes AM, Strauss JL (1998) Dynamic systems theory as a paradigm for the study of change in psychotherapy: An application to cognitive therapy for depression. *J Consult Clin Psychol* 66(6):939–947.
12. Heiby EM, Pagano IS, Blaine DD, Nelson K, Heath RA (2003) Modeling unipolar depression as a chaotic process. *Psychol Assess* 15(3):426–434.
13. de Wild-Hartmann JA, et al. (2013) Day-to-day associations between subjective sleep and affect in regard to future depression in a female population-based sample. *Br J Psychiatry* 202(6):407–412.
14. Wichers M, et al. (2007) Genetic risk of depression and stress-induced negative affect in daily life. *Br J Psychiatry* 191(3):218–223.
15. Wichers M (2013) The dynamic nature of depression: A new micro-level perspective of mental disorder that meets current challenges. *Psychol Med* 14:1–12.
16. Bringmann LF, et al. (2013) A network approach to psychopathology: New insights into clinical longitudinal data. *PLoS One* 8(4):e60188.
17. Tzur-Bitan D, Meiran N, Steinberg DM, Shahar G (2012) Is the looming maladaptive cognitive style a central mechanism in the (generalized) anxiety–(major) depression comorbidity: An intra-individual, time series study. *Int J Cogn Ther* 5(2):170–185.
18. Keller MC, Neale MC, Kendler KS (2007) Association of different adverse life events with distinct patterns of depressive symptoms. *Am J Psychiatry* 164(10):1521–1529, quiz 1622.
19. Cramer AO, Borsboom D, Aggen SH, Kendler KS (2012) The pathoplasticity of dysphoric episodes: Differential impact of stressful life events on the pattern of depressive symptom inter-correlations. *Psychol Med* 42(5):957–965.
20. Lux V, Kendler KS (2010) Deconstructing major depression: A validation study of the DSM-IV symptomatic criteria. *Psychol Med* 40(10):1679–1690.
21. Cramer AOJ, et al. (2012) Dimensions of normal personality as networks in search of equilibrium: You can't like parties if you don't like people. *Eur J Pers* 26(4):414–431.
22. Kim NS, Ahn WK (2002) Clinical psychologists' theory-based representations of mental disorders predict their diagnostic reasoning and memory. *J Exp Psychol Gen* 131(4):451–476.
23. Frewen PA, Allen SL, Lanius RA, Neufeld RWJ (2012) Perceived causal relations: Novel methodology for assessing client attributions about causal associations between variables including symptoms and functional impairment. *Assessment* 19(4):480–493.
24. Frewen PA, Schmittmann VD, Bringmann LF, Borsboom D (2013) Perceived causal relations between anxiety, posttraumatic stress and depression: Extension to moderation, mediation, and network analysis. *Eur J Psychotraumatol* 4:20656.
25. Scheffer M (2009) *Critical Transitions in Nature and Society* (Princeton Univ Press, Princeton).
26. Patten SB (2013) Major depression epidemiology from a diathesis-stress conceptualization. *BMC Psychiatry* 13:19.
27. Scheffer M, et al. (2009) Early-warning signals for critical transitions. *Nature* 461(7260):53–59.
28. Scheffer M, et al. (2012) Anticipating critical transitions. *Science* 338(6105):344–348.
29. Dakos V, et al. (2008) Slowing down as an early warning signal for abrupt climate change. *Proc Natl Acad Sci USA* 105(38):14308–14312.
30. Carpenter SR, et al. (2011) Early warnings of regime shifts: A whole-ecosystem experiment. *Science* 332(6033):1079–1082.
31. Carpenter SR (2003) *Regime Shifts in Lake Ecosystems: Pattern and Variation* (International Ecology Institute, Oldendorf, Germany).
32. Strogatz S (1994) *Nonlinear Dynamics and Chaos: With Applications to Physics, Biology, Chemistry and Engineering* (Perseus, New York).
33. van Nes EH, Scheffer M (2007) Slow recovery from perturbations as a generic indicator of a nearby catastrophic shift. *Am Nat* 169(6):738–747.
34. Veraart AJ, et al. (2012) Recovery rates reflect distance to a tipping point in a living system. *Nature* 481(7381):357–359.
35. Dai L, Vorselen D, Korolev KS, Gore J (2012) Generic indicators for loss of resilience before a tipping point leading to population collapse. *Science* 336(6085):1175–1177.
36. Carpenter SR, Brock WA (2006) Rising variance: A leading indicator of ecological transition. *Ecol Lett* 9(3):311–318.
37. Drake JM, Griffen BD (2010) Early warning signals of extinction in deteriorating environments. *Nature* 467(7314):456–459.
38. Chen L, Liu R, Liu Z-P, Li M, Aihara K (2012) Detecting early-warning signals for sudden deterioration of complex diseases by dynamical network biomarkers. *Sci Rep* 2:342.
39. Russell JA (2003) Core affect and the psychological construction of emotion. *Psychol Rev* 110(1):145–172.
40. Pe ML, Kuppens P (2012) The dynamic interplay between emotions in daily life: Augmentation, blunting, and the role of appraisal overlap. *Emotion* 12(6):1320–1328.
41. Wichers M, Lothmann C, Simons CJP, Nicolson NA, Peeters F (2012) The dynamic interplay between negative and positive emotions in daily life predicts response to treatment in depression: A momentary assessment study. *Br J Clin Psychol* 51(2):206–222.
42. Watson D, Clark LA, Tellegen A (1988) Development and validation of brief measures of positive and negative affect: The PANAS scales. *J Pers Soc Psychol* 54(6):1063–1070.
43. Dakos V, et al. (2012) Methods for detecting early warnings of critical transitions in time series illustrated using simulated ecological data. *PLoS One* 7(7):e41010.
44. Dakos V, van Nes EH, D'Odorico P, Scheffer M (2012) Robustness of variance and autocorrelation as indicators of critical slowing down. *Ecology* 93(2):264–271.
45. Kuppens P, Allen NB, Sheeber LB (2010) Emotional inertia and psychological maladjustment. *Psychol Sci* 21(7):984–991.
46. Kuppens P, et al. (2012) Emotional inertia prospectively predicts the onset of depressive disorder in adolescence. *Emotion* 12(2):283–289.
47. Kéfi S, Dakos V, Scheffer M, Van Nes EH, Rietkerk M (2012) Early warning signals also precede non-catastrophic transitions. *Oikos* 122(5):641–648.
48. Csikszentmihalyi M, Larson R (1987) Validity and reliability of the Experience-Sampling Method. *J Nerv Ment Dis* 175(9):526–536.
49. Myin-Germeys I, et al. (2009) Experience sampling research in psychopathology: Opening the black box of daily life. *Psychol Med* 39(9):1533–1547.
50. StataCorp (2009) *Stata Statistical Software* (StataCorp LP, College Station, TX).
51. R Development Core Team (2005) *R: A Language and Environment for Statistical Computing* (R Foundation for Statistical Programming, Vienna).
52. Hox J (2010) *Multilevel Analysis: Techniques and Applications*, Quantitative Methodology Series (Routledge, New York), 2nd Ed.
53. van Nes EH, Scheffer M (2004) Large species shifts triggered by small forces. *Am Nat* 164(2):255–266.

Supplementary Information to

Critical slowing down as early warning for the onset and termination of depression

van de Leemput et al. PNAS

Figures

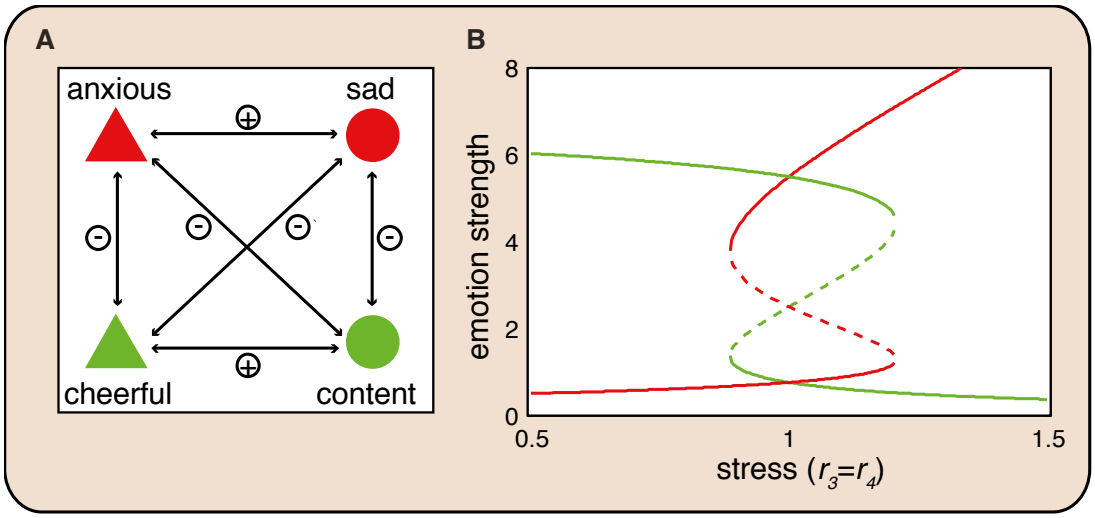

Fig. S1. The model. (**A**) A graphical representation of our simple dynamical model of four emotions. Emotions with the same valence have a positive effect on each other, while emotions of different valence have a strong negative effect on each other. (**B**) The stability properties of the deterministic part of the model (i.e. without noise) change if stress levels, represented by the growth rate of the two negative emotions (r_3 and r_4), change. Green lines represent positive emotions (x_1 and x_2), red lines represent negative emotions (x_3 and x_4). Solid lines represent stable states, and dashed lines unstable states. Far from the tipping point, at low stress levels, the network has only one stable state with high levels of positive emotions, and low levels of negative emotions. If stress levels increase, the network has two stable states: a 'normal state', and a 'depressed state', while at even higher stress levels, the system reaches a tipping point, at which the normal state disappears, and only one stable depressed state remains. Note that once the system is in the alternative depressed state, stress levels need to be decreased tremendously to trigger a backward shift.

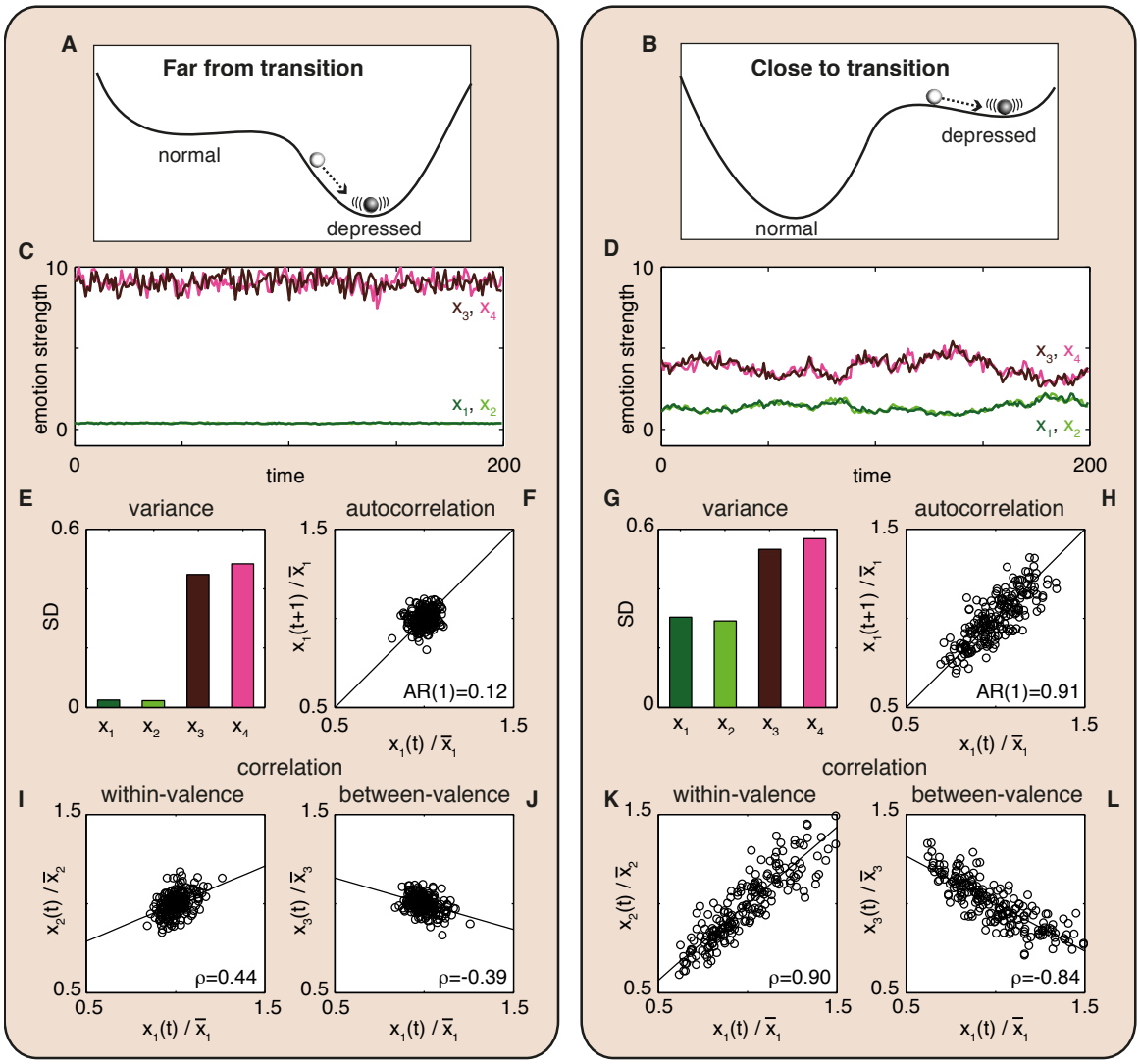

Fig. S2. Model simulations illustrating generic indicators of proximity to a tipping point from a depressed to normal state. Our model shows that the generic early warning signals that signal the proximity of a shift from a normal state towards a depressed state are also valid for the backward shift from a depressed state towards recovery. In that case, the stability of a depressed person may become more fragile close to the transition towards recovery (**B versus A**). Under a permanent regime of stochastic perturbations (**C and D**), slowing down near the tipping point results in higher variance (SD= standard deviation) (**G versus E**), higher temporal autocorrelation (AR(1)= lag-1 autoregression coefficient) (**H versus F**), and stronger correlation (ρ= Pearson correlation coefficient) between emotions with the same valence (**K versus I**), and between emotions with different valence (**L versus J**). Positive emotions are represented by x_1 and x_2, and negative emotions by x_3 and x_4. Parameters: left panels $r_3=r_4=1.5$, right panels $r_3=r_4=0.9$.

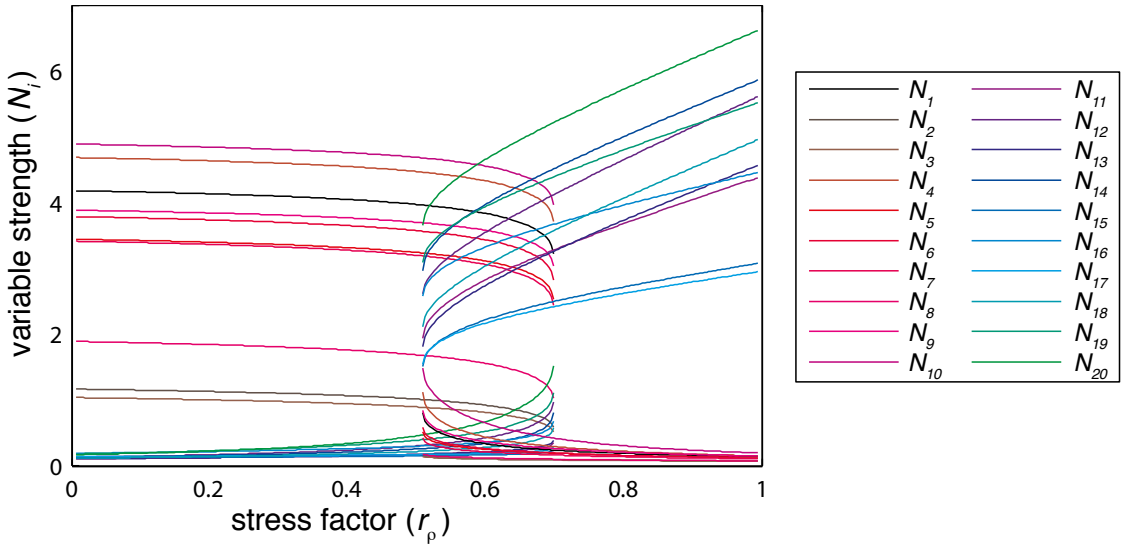

Fig. S3. Response of the network model to stress. The stability properties of the deterministic part of the model (i.e. without noise) change if stress levels, represented by r_ρ, change. Solid lines represent stable states, unstable states are not depicted. Far from the tipping point, at low stress levels, the network has only one stable state with one dominant cluster of network elements: the 'normal state'. If stress levels increase, the network has two stable states. Next to the 'normal state', another cluster can be dominant under the same conditions: the 'depressed state'. At even higher stress levels, the system reaches a tipping point, at which the normal state disappears, and only one stable depressed state remains.

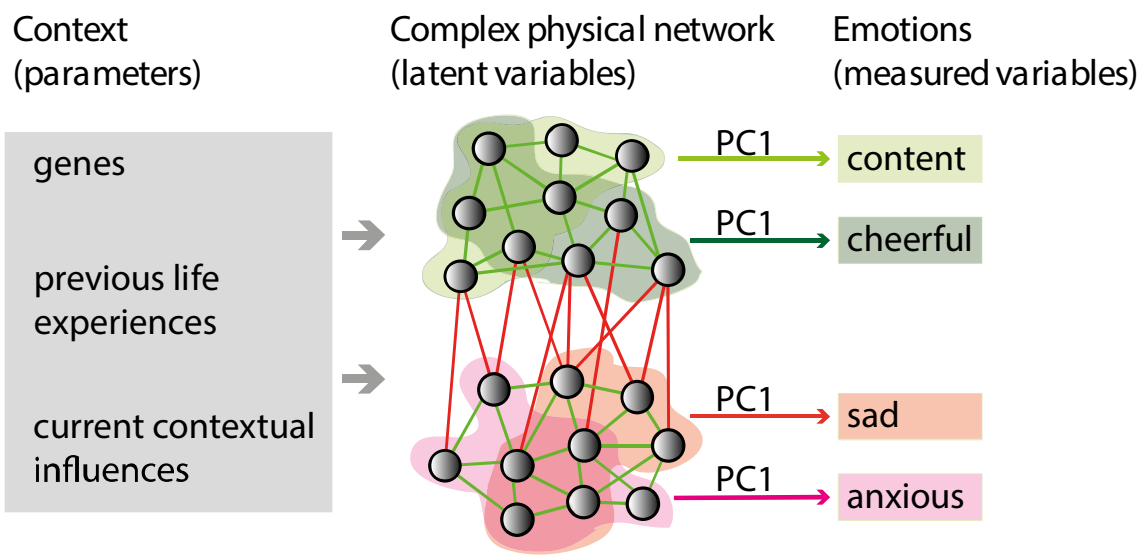

Figure S4. Illustration of the relation between the context, the complex physical network model (e.g. elements ranging from neurotransmitter and hormone concentrations to physical activity modes and social interactions) and the four newly defined variables. Note that the four variables are indirect indicators of parts of the complex system.

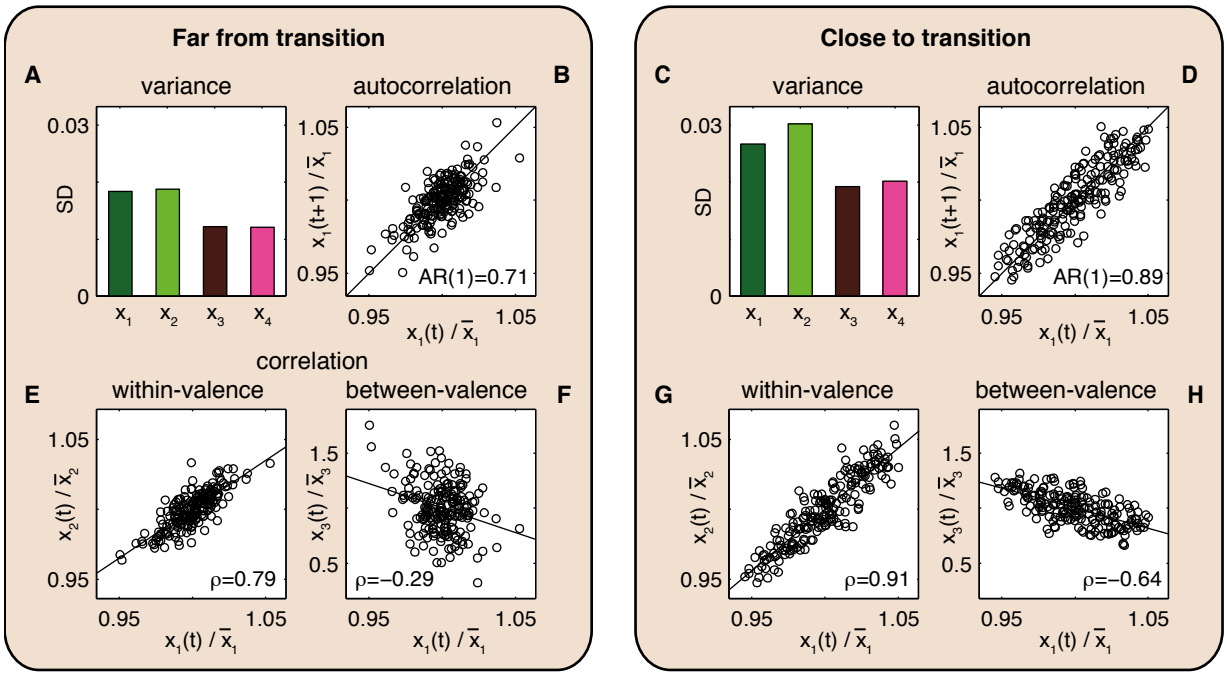

Fig. S5. Early warning signal analysis of model simulations of the four indirect indicators of the complex network. As for the four-component model with direct interactions, under a permanent regime of stochastic perturbations, slowing down near the tipping point results in higher variance (SD= standard deviation) (**A versus C**), higher temporal autocorrelation (AR(1)= lag-1 autoregression coefficient) (**B versus D**), and stronger correlation (ρ= Pearson correlation coefficient) between emotions with the same valence (**E versus G**), and between emotions with different valence (**F versus H**). Positive emotions are represented by x_1 and x_2, and negative emotions by x_3 and x_4. Parameters: left panels r_ρ=0.1, right panels r_ρ=0.68.

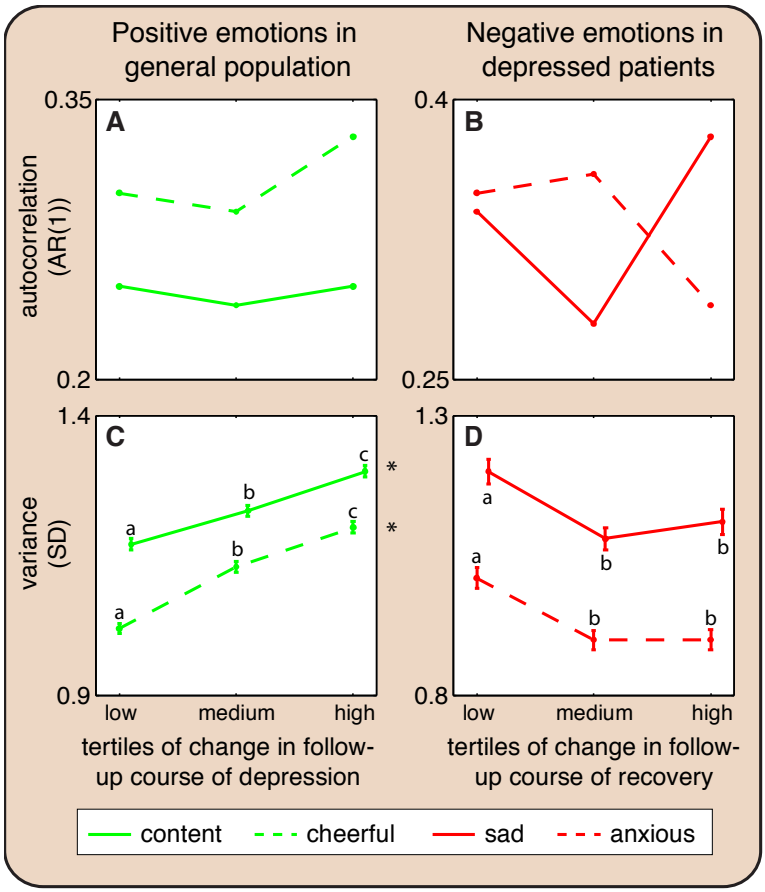

Fig. S6. Temporal autocorrelation and variance as a function of future symptoms. Increasing autocorrelation (AR(1) = mean lag-1 autoregression coefficient) (**A and B**) and variance (SD = mean standard deviation) (**C and D**) of positive emotions according to tertiles of development of future depressive symptoms in a general population (left panels), and of negative emotions according to tertiles of future recovery in depressed patients (right panels). For autocorrelation (**A and B**), we present data according to tertiles of change in follow-up course for illustrative purposes only, however, note that in the statistical analyses continuous variables were used. There are no significant trends in autocorrelation (positive interaction effect of future symptoms: $p<0.05$). For variance (**C and D**), error bars represent standard errors (SEs). Note that variance of negative emotions in the depressed population goes down with future recovery. This may be explained by differences in the mean (see Fig. S7). Asterisks indicate an overall significant upward trend in variance (overall tests: $p<0.05$). Mean values represented by different letters within emotions are significantly different (post-hoc tests: $p<0.05$).

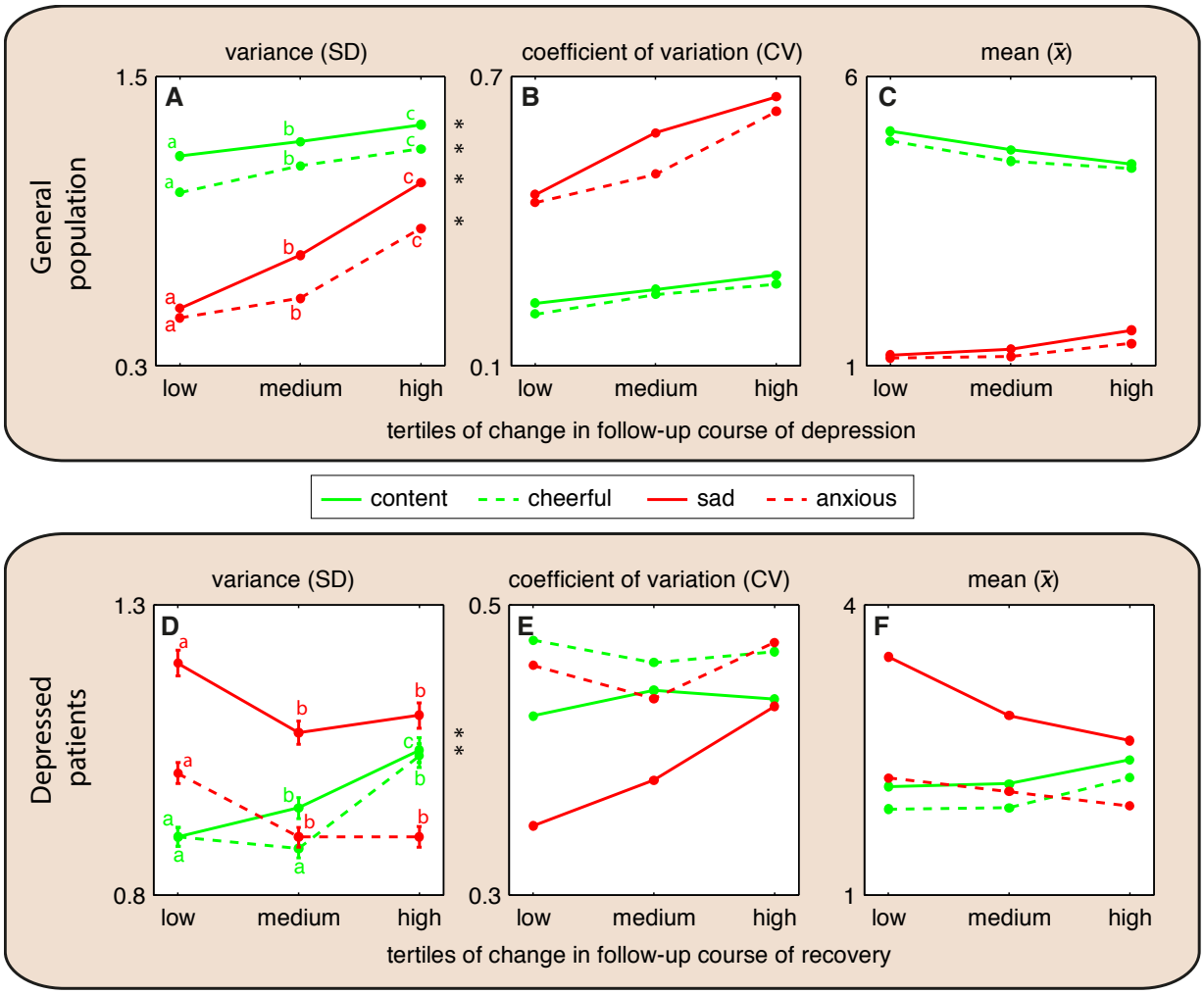

Fig. S7. The effect of critical slowing down on variance can be confounded by a change in the means. Variance (SD = mean standard deviation) (**A and D**), coefficient of variation (CV=SD/$\bar{x}$) (**B and E**), and mean affect level ($\bar{x}$) (**C and F**) according to tertiles of development of future depressive symptoms in a general population (n=535) (**upper panels**), and according to tertiles of future recovery in depressed patients (n=93) (**lower panels**). Note that for the general population, higher variance in individuals with higher future recovery is robust if corrected for the means, while for the depressed population, both higher variance of positive emotions, and lower variance of negative emotions, are not robust.

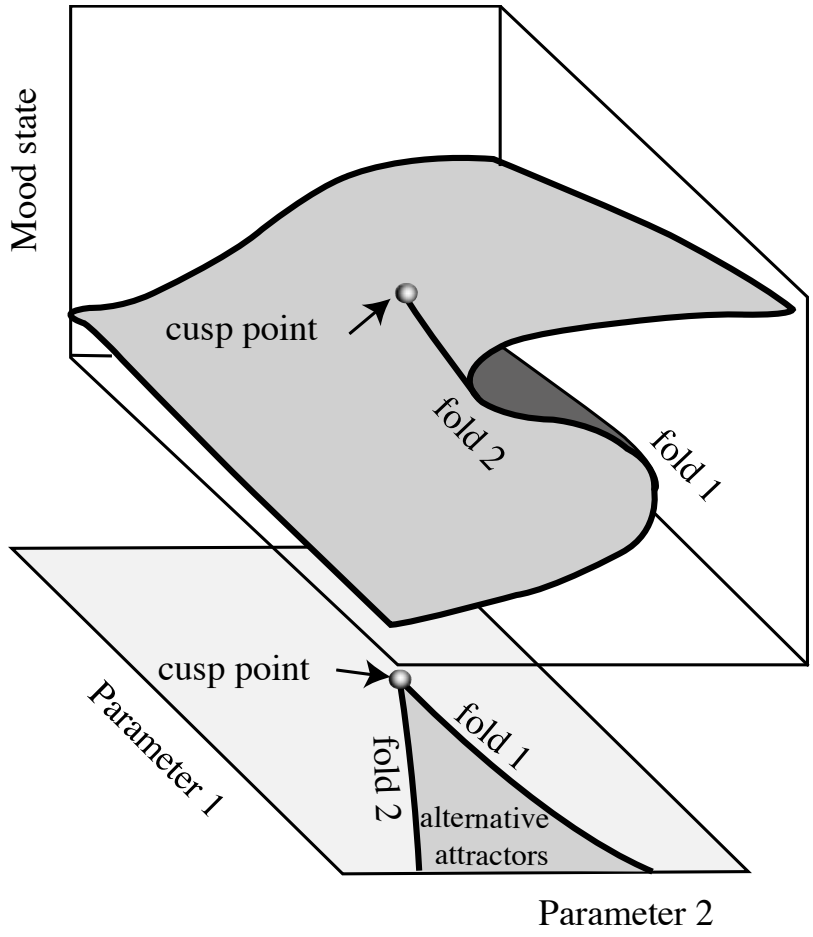

Fig. S8. The response of a dynamical system to a stressor (e.g. parameter 2) may be smooth or catastrophic depending on the strength of a positive feedback (e.g. parameter 1).The cusp point defines the parameter settings at which the system changes from smooth to catastrophic. The fold bifurcations define the parameter settings at which the system changes from two alternative stable states to one.

Tables

Table S1a. The socio-demographic and depression-related characteristics for the general population sample.

General population sample (n=535)			
	Mean (SD) or percentage	n (individuals) N (observations)	
Age	27.6 (7.8)	n=534	
Female gender	100%	n=535	
No/only primary school education	1%	n=4	
Secondary school education only	1%	n=6	
Intermediate vocational education	34%	n=184	
College/University	64%	n=341	
Baseline SCL-90-R (item average)	1.44 (0.51)	n=535	
Average follow-up SCL-90-R (item average)	1.47 (0.48)	n=535	
Baseline average rating (1-7) of *cheerful*	4.63 (0.86)	n=535	N=19,752
Baseline average rating (1-7) of *content*	4.77 (0.86)	n=535	N=19,660
Baseline average rating (1-7) of *anxious*	1.22 (0.38)	n=535	N=19,673
Baseline average rating (1-7) of *sad*	1.35 (0.52)	n=535	N=19,732
Average follow-up SCL-90-R per tertile (low, medium or high follow-up score)	low: 1.08 (0.06) n= 182	medium: 1.33 (0.09) n= 177	high: 2.02 (0.48) n=176
Baseline average rating (1-7) of *cheerful* per tertile of follow-up SCL-90-R score	4.90 (0.90)	4.54 (0.80)	4.43 (0.81)
Baseline average rating (1-7) of *content* per tertile of follow-up SCL-90-R score	5.07 (0.85)	4.73 (0.81)	4.51 (0.83)
Baseline average rating (1-7) of *anxious* per tertile of follow-up SCL-90-R score	1.13 (0.31)	1.16 (0.24)	1.38 (0.49)
Baseline average rating (1-7) of *sad* per tertile of follow-up SCL-90-R score	1.18 (0.43)	1.30 (0.41)	1.59 (0.62)

Table S1b. The socio-demographic and depression-related characteristics for the depressed patient sample.

Depressed patients (n=93)			
	Mean (SD) or percentage	n (individuals) N (observations)	
Age	41.7 (9.9)	n=93	
Female gender	40%	n=93	
No/only primary school education	19%	n=18	
Secondary school education only	27%	n=25	
Intermediate vocational education	39.8%	n=37	
College/University	10.8%	n=10	
Baseline HDRS-17 total score	24.0 (3.7)	n=93	
Follow-up HDRS-17 total score	12.5 (6.8)	n=93	
Baseline average rating (1-7) of *cheerful*	1.96 (0.92)	n=93	N=4.250
Baseline average rating (1-7) of *content*	2.19 (1.03)	n=93	N=4.270
Baseline average rating (1-7) of *anxious*	2.03 (1.40)	n=93	N=4.275
Baseline average rating (1-7) of *sad*	3.00 (1.32)	n=93	N=4.282
Intervention following baseline: **-combination of pharmacotherapy and supportive psychotherapy** **-imipramine (as part of a trial)** **-placebo (as part of a trial)**		n= 43 n=23 n=27	
Average follow-up HDRS-17 per tertile of change in follow-up HDRS-17 score (low, medium or high reduction in symptoms)	low: 19.1 (3.5) n= 33	medium: 12.2 (4.4) n= 32	high: 5.7 (3.4) n=28
Baseline average rating of *cheerful* per tertile of change in follow-up HDRS-17 score	1.87 (0.77)	1.90 (0.82)	2.15 (1.15)
Baseline average rating of *content* per tertile of change in follow-up HDRS-17 score	2.09 (0.92)	2.17 (0.94)	2.32 (1.24)
Baseline average rating of *anxious* per tertile of change in follow-up HDRS-17 score	2.17 (1.50)	1.97 (1.31)	1.93 (1.43)
Baseline average rating of *sad* per tertile of change in follow-up HDRS-17 score	3.51 (1.34)	2.79 (1.14)	2.62 (1.35)

Table S2. Regression analysis in which the interaction effect represents the extent to which autoregression coefficients increase with increased follow-up change in depressive symptoms.

Autocorrelation				
	General population		*Depressed patients*	
	Beta-coefficient of interaction effect size[α]	p-value	Beta-coefficient of interaction effect size[β]	p-value
Cheerful	0.014	0.537	0.008	0.017
Content	-0.007	0.738	0.006	0.100
Anxious	0.060	0.029	-0.002	0.662
Sad	0.065	0.024	0.005	0.135

α: follow-up average SCL-90-R depression score X 'emotion' moment (t-1) on 'emotion' moment (t)

β: decrease in HDRS-17 score from baseline to follow-up X 'emotion' moment (t-1) on 'emotion' moment (t)

Table S3a. The overall significance tests for differences between variances across the three tertile groups for the general population and the depressed patients.

Variance									
General population									
	Low FU symptoms		Medium FU symptoms		High FU symptoms		Overall Wald test		
	Coeff	SE	Coeff	SE	Coeff	SE	χ^2	df	p-value
Cheerful	1.02	0.009	1.13	0,01	1.20	0.010	165.52	2	<0.001
Content	1.17	0.010	1.23	0,01	1.30	0.010	68.13	2	<0.001
Anxious	0.50	0.004	0.58	0,005	0.87	0.008	1761.48	2	<0.001
Sad	0.54	0.005	0.76	0,007	1.06	0.009	2623.37	2	<0.001
Depressed patients									
	Low decrease in FU symptoms		Medium decrease in FU symptoms		High decrease in FU symptoms		Overall Wald test		
	Coeff	SE	Coeff	SE	Coeff	SE	χ^2	df	p-value
Cheerful	0.90	0.016	0.88	0.016	1.04	0.021	41.41	2	<0.001
Content	0.90	0.016	0.95	0.018	1.05	0.021	31.92	2	<0.001
Anxious	1.01	0.018	0.90	0.017	0.90	0.018	23.56	2	<0.001
Sad	1.20	0.022	1.08	0.020	1.11	0.022	17.16	2	<0.001

Table S3b. P-values of the post-hoc Wald tests for differences between variances across the three tertile groups for the general population and the depressed patients.

Variance			
General population			
	Low vs Medium FU symptoms	Low vs High FU symptoms	Medium vs High FU symptoms
Cheerful	<0.001	<0.001	<0.001
Content	<0.001	<0.001	<0.001
Anxious	<0.001	<0.001	<0.001
Sad	<0.001	<0.001	<0.001
Depressed patients			
	Low vs Medium decrease in FU symptoms	Low vs High decrease in FU symptoms	Medium vs High decrease in FU symptoms
Cheerful	0.337	<0.001	<0.001
Content	0.049	<0.001	<0.001
Anxious	<0.001	<0.001	0.883
Sad	<0.001	0.005	0.278

Table S4a. The overall significance tests for differences between correlations across the three tertile groups for the general population and the depressed patients.

Correlation									
General population									
	Low FU symptoms		Medium FU symptoms		High FU symptoms		Overall Wald test		
	Coeff	SE	Coeff	SE	Coeff	SE	χ^2	df	p-value
Anxious-sad	0.25	0.012	0.26	0.011	0.34	0.012	34.13	2	<0.002
Cheerful-content	0.50	0.009	0.54	0.009	0.56	0.009	22.19	2	<0.001
Anxious-cheerful	-0.16	0.012	-0.19	0.012	-0.21	0.012	10.20	2	0.006
Anxious-content	-0.19	0.012	-0.24	0.012	-0.28	0.012	26.54	2	<0.001
Sad-cheerful	-0.30	0.011	-0.35	0.011	-0.41	0.011	44.89	2	<0.001
Sad-content	-0.28	0.011	-0.34	0.011	-0.39	0.011	51.52	2	<0.001
Depressed patients									
	Low decrease in FU symptoms		Medium decrease in FU symptoms		High decrease in FU symptoms		Overall Wald test		
	Coeff	SE	Coeff	SE	Coeff	SE	χ^2	df	p-value
Anxious-sad	0.30	0.024	0.32	0.024	0.37	0.024	5.09	2	0.078
Cheerful-content	0.47	0.020	0.52	0.019	0.61	0.018	25.79	2	<0.001
Anxious-cheerful	-0.10	0.026	-0.12	0.026	-0.27	0.026	25.34	2	<0.001
Anxious-content	-0.14	0.026	-0.12	0.026	-0.22	0.027	8.19	2	0.017
Sad-cheerful	-0.30	0.024	-0.35	0.023	-0.43	0.023	16.82	2	<0.001
Sad-content	-0.31	0.023	-0.35	0.023	-0.36	0.025	2.20	2	0.332

Table S4b. P-values of the post-hoc Wald tests for differences between correlations across the three tertile groups for the general population and the depressed patients.

Correlation			
General population			
	Low vs Medium FU symptoms	Low vs High FU symptoms	Medium vs High FU symptoms
Anxious-sad	0.294	<0.001	<0.001
Cheerful-content	0.001	<0.001	0.225
Anxious-cheerful	0.107	0.001	0.112
Anxious-content	0.002	<0.001	0.032
Sad-cheerful	0.002	<0.001	<0.001
Sad-content	<0.001	<0.001	<0.001
Depressed patients			
	Low vs Medium decrease in FU symptoms	Low vs High decrease in FU symptoms	Medium vs High decrease in FU symptoms
Anxious-sad	0.478	0.027	0.129
Cheerful-content	0.075	<0.001	0.001
Anxious-cheerful	0.694	<0.001	<0.001
Anxious-content	0.659	0.024	0.007
Sad-cheerful	0.164	<0.001	0.008
Sad-content	0.249	0.168	0.787

Text

Text S1. Network model of latent variables

We developed a network model that serves as a hypothetical representation of the complex neurobiological system underlying the mood of an individual person. The network consists of twenty interacting latent variables. Each network variable represents one (unknown, but in principle measurable) component of the neurobiological system of that individual. Emotions are not represented directly as variables but are computed as principal components of simulation results of clusters of the network. In contrast with the simple model in the main text, they do not interact directly with each other. We demonstrate that such indirect indicators show the same behaviour in terms of early warning signals.

The network model was also based on the Lotka-Volterra model, describing the dynamics of interacting variables, representing the components of the neurobiological system:

$$\frac{dN_i}{dt} = r_i N_i + \sum_j^{20} C_{i,j} N_j N_i + \epsilon_N + \mu$$

where N_i represents the strength of network variable i, r_i represents the maximum rate of change of network variable i, C represents a matrix of interactions between network variables, μ represents a small continuous increase of the strength of a network variable (independent of their state) (μ=1), and ϵ_N is the stochastic part of the model represented by a Gaussian white noise process of mean zero and intensity σ^2/dt (σ=0.1) (i.e. additive noise).

We parameterized the network such that the system has two main clusters: network variables that are in the same cluster have a positive effect on each other, while variables of different clusters have a negative effect. The interaction strengths $C_{i,j}$, as well as the maximum rate of change (r_i), were randomly drawn from two uniform distributions. Positive interactions between network variables within a predefined cluster ranged from 0.003 to 0.005. Similarly, the negative interactions between variables of different clusters were drawn in a range between -0.002 and -0.004. The maximum relative rates of change (r_i) of the individual variables were assumed to be stress dependent, following:

$$r_i = r_{0,i} + r_\rho \rho_i$$

Maximum rates of change of network variables in a state without stress (r_0) are set to differ between the two clusters. In cluster 1 r_0 ranges from 0 to 1, while in cluster 2 r_0 ranges from 0 to 0.5. Stress is assumed

to influence the maximum rates by a factor r_ρ. Each network variable has a different sensitivity (ρ) to this stress factor. The sensitivity of variables in cluster 1 is assumed to be 0, while the sensitivity of variables in cluster 2 ranges from 0 to 1. For these parameter settings, this complex network has alternative stable states (Fig. S3).

In order to define four relevant indicators of dynamics in the network, we assume that each emotion is influenced by the dynamics of a subcluster of the network: each positive emotion is determined by seven of the ten variables of cluster 1, while each negative emotion is determined by seven of the ten variables of cluster 2 (Fig. S4). The subclusters that define the new variables contain overlapping network variables. Therefore, we simulated two time series with a different dominant cluster. We used each time series to perform two PCA analyses on seven variables of the dominant cluster. We used the first principal component (*PC1*) of each analysis to define the dynamics of the four new variables (x). For instance, the first variable (x_1) is defined as follows:

$$x_1 = \sum_j^7 PC1_j N_j$$

We simulated the dynamics of the complete model, and used the data of the four variables as input for the early warning signal analysis, as in the main text.

Importantly, in our network model, the four variables representing emotion strength (x) do not directly affect each other, they are simply indicators of the dynamics of a complex underlying network (Fig. S4). Our analyses show that the same early warning signals are expected if the variables are indirect indicators of a complex underlying system with tipping points between alternative stable state (Fig. S5). The predictions of critical slowing down are thus robust against this oversimplified way of representing emotions in the model of the main text.

Text S2. Supplementary methods

Inclusion criteria and final set of participants. Inclusion criteria in both studies were a DSM-IV diagnosis of major depressive disorder (MDD), age between 18 and 65 years, and a baseline score of ≥18 on the 17-item HDRS. Patients using psychotropic medications, other than low dose benzodiazepines, were excluded (1, 2). Of the 621 individuals of the general population sample, only 610 participated in ESM. Of this group 31 were excluded because of too few valid ESM measurements (3). Forty-four participants had missing data either at baseline or follow-up resulting in 535 individuals. In the depressed sample 118 were eligible to participate. Of those, six were excluded because of too few valid ESM measurements and 1 because of unavailability of emotion ratings in ESM. Additionally, 1 had missing baseline data and 17 had missing follow-up HDRS measurements. This resulted in a final sample of 93 participants.

Heteroscedasticity and normality. The current samples have 535 and 93 groups (individuals) with on average 37 and 45 observations, respectively, per individual. When checking our data, two main assumptions of the model did not hold for some of the analyses: homoscedasticity at level 1 (i.e., the variability of residuals within persons may differ from one person to the other) and normality (i.e., the distribution of scores within a person may not be normal). Violations of these assumptions were found through the inspection of residual plots. Estimates in the models may be slightly downwardly biased if the number of groups (level 2 units) is less than 50 and the normality assumption is violated. According to Hox (4) at least 50 level 2 groups (in this case individuals) are needed with 20 or more observations within each group in order to accurately estimate standard errors in case of violation of the normality assumption. Thus, according to Hox (4), the current sample sizes are adequate to yield accurate estimations of standard errors.

In order to test the potential influence of heteroscedasticity, all analyses were repeated with robust standard errors (using the so-called Huber–White or sandwich standard errors). These analyses yielded similar results and conclusions.

Estimating the potential function. We have considered the possibility to directly estimate the potential function. However, although the methodology is developed for a long time series (see e.g (5, 6)), the extension to our case is far from trivial. The reason is that the data consist of a sample of quite short time series, which do not yield enough information for estimating a person-specific potential function that is flexible enough (i.e., not restricted to a specific parametric form). In principle, this would be possible by setting up the estimation problem in the aforementioned multilevel modeling framework. However, this is a completely new methodology that has not been developed, let alone be sufficiently tested. Therefore, we have refrained in this paper from estimating the potential function.

Text S3. Individual and group responses

All people differ in their response to changing conditions and in their underlying emotional vulnerability. For each individual the dynamic interplay between emotions may differ. For example, some individuals quickly become anxious if something happens that makes them sad, while others don't have a strong connection between these two emotions (7). This may explain why some people slowly glide into a depression, while others shift much more suddenly and unexpectedly (Fig. S8). The result of the complex interplay between the multiple different emotional states people experience may thus differ from individual to individual and may impact on moment and timing of transition. We can hypothesize that the critical moment and speed with which a system may shift to another level of depressive symptoms is different per individual. When data of many different individuals are grouped together we expect *–at group level-* early warning signals to be associated with a dimensional change in depressive symptoms (since every system has its own point to shift), which is a reason for not categorizing by diagnosis status. This also illustrates a second reason: we do not necessarily expect that transition moments coincide with man-made arbitrary DSM-IV criteria. For some individuals critical shifts may occur at subclinical levels while for other individuals shifts occur to clinical levels of depression. As explained above each individual likely has his/her own mood set points and thresholds for tipping points, and some may even have no thresholds at all, but simply a smooth response to changing conditions. The results of the study support this view on transitions since indicators of critical slowing down predicted dimensional transitions towards higher or lower levels of depressive symptoms.

References

1. Peeters F, Nicolson NA, Berkhof J, Delespaul P, deVries M (2003) Effects of daily events on mood states in major depressive disorder. *J Abnorm Psychol* 112(2):203-211.
2. Barge-Schaapveld DQ, Nicolson NA, van der Hoop RG, De Vries MW (1995) Changes in daily life experience associated with clinical improvement in depression. *J Affect Disord* 34(2):139-154.
3. Delespaul P (1995) *Assessing schizophrenia in daily life: The experience sampling method* (University of Limburg, Maastricht)
4. Hox J (2010) *Multilevel analysis: techniques and applications (Quantitative Methodology Series)* (Routledge, New York) 2nd Ed
5. Brillinger DR (2007) Learning a potential function from a trajectory. *IEEE Signal Processing Letters* 14(12):1-4.
6. Wagenmakers E-J, Molenaar PCM, Grasman RPPP, Hartelman PaI, van der Maas HLJ (2005) Transformation invariant stochastic catastrophe theory. *Physica D* 211(3-4):263-276.
7. Wigman JTW, et al. (2013) Psychiatric diagnosis revisited: towards a system of staging and profiling combining nomothetic and idiographic parameters of momentary mental states. *PLoS ONE* 8(3):e59559-e59559.

```
# Download and install R on your computer (from http://www.r-project.org/).
# Install the following packages: lme4 and foreign as follows:
#    install.packages("lme4")
#    install.packages("foreign")
#
# Put all data files (reshape_corr_patients.csv, data_patients.csv, reshape_corr_twin.csv,
#                     data_twins.csv, results_dep.txt, results_gen.txt)
#    and this file with R code in a directory.
# This directory will become your working directory.

setwd("C:\\Folder\\Subfolder") # set this to your working directory

require(lme4)
require(nlme)
require(foreign)

############################
### DEPRESSED SAMPLE #######
############################

#####################################################################
### variance and correlation analysis for depressed patients #######
#####################################################################

rm(list=ls())

dat <- read.table("reshape_corr_patients.csv", header=TRUE, sep=",")
dat <- dat[order(dat$subjno),]
dat$beep <- rep(sequence(sapply(split(dat$subjno, dat$subjno), length)/4), each=4)

### hdrs_tert==1
res1 <- lme(affect ~ dum_opg + dum_tev + dum_ang + dum_som - 1,
            random = ~ factor(item) - 1 | subjno,
            weights = varIdent(form = ~ 1 | item),
            correlation = corSymm(form = ~ 1 | subjno/beep),
            data=dat, na.action=na.omit,
            control=list(msVerbose=TRUE, maxIter=500, msMaxIter=500), subset=hdrs_tert==1)
summary(res1)

### hdrs_tert==2
res2 <- lme(affect ~ dum_opg + dum_tev + dum_ang + dum_som - 1,
            random = ~ factor(item) - 1 | subjno,
            weights = varIdent(form = ~ 1 | item),
            correlation = corSymm(form = ~ 1 | subjno/beep),
            data=dat, na.action=na.omit,
            control=list(msVerbose=TRUE, maxIter=500, msMaxIter=500), subset=hdrs_tert==2)
summary(res2)

### hdrs_tert==3
res3 <- lme(affect ~ dum_opg + dum_tev + dum_ang + dum_som - 1,
            random = ~ factor(item) - 1 | subjno,
            weights = varIdent(form = ~ 1 | item),
            correlation = corSymm(form = ~ 1 | subjno/beep),
            data=dat, na.action=na.omit,
            control=list(msVerbose=TRUE, maxIter=500, msMaxIter=500), subset=hdrs_tert==3)
summary(res3)

#########################################################
### autocorrelation analysis for depressed patients #######
#########################################################

rm(list=ls())
dat2 <- read.table("data_patients.csv", header=TRUE, sep=";")

################
### cheerful ###
################

### hdrs_change as linear term
auto1lmer <- lmer(opgew_dev ~ opgewkt_dl*hdrs_change + (-1+opgewkt_dl|subjno),
                  control=list(msVerbose=TRUE, maxIter=500), data=dat2, na.action=na.exclude, REML=FALSE)
summary(auto1lmer)

auto1lmer <- lme(opgew_dev ~ opgewkt_dl*hdrs_change, random = ~ -1+opgewkt_dl|subjno,
                 control=list(msVerbose=TRUE, maxIter=500), data=dat2, na.action=na.exclude, method="ML")
summary(auto1lmer)

### hdrs_tert = tertiles
auto1lmerT <- lmer(opgew_dev ~ opgewkt_dl*factor(hdrs_tert) + (-1+opgewkt_dl|subjno),
                   control=list(msVerbose=TRUE, maxIter=500), data=dat2, na.action=na.exclude)
summary(auto1lmerT)
auto1lmerT@fixef[2]+c(0,auto1lmerT@fixef[5:6])

################
### content  ###
################
```

```
### hdrs_change as linear term
auto2lmer<-lmer(tevr_dev ~ tevreden_dl*hdrs_change + (-1+tevreden_dl|subjno),
                control=list(msVerbose=TRUE, maxIter=500),data=dat2,na.action=na.exclude, REML=FALSE)
summary(auto2lmer)

### hdrs_tert = tertiles
auto2lmerT<-lmer(tevr_dev ~ tevreden_dl*factor(hdrs_tert) + (-1+tevreden_dl|subjno),
                 control=list(msVerbose=TRUE, maxIter=500),data=dat2,na.action=na.exclude, REML=FALSE)
summary(auto2lmerT)
auto2lmerT@fixef[2]+c(0,auto2lmerT@fixef[5:6])

################
### anxious  ###
################

### hdrs_change as linear term
auto3lmer<-lmer(ang_dev ~ angstig_dl*hdrs_change + (-1+angstig_dl|subjno),
                control=list(msVerbose=TRUE, maxIter=500),data=dat2,na.action=na.exclude, REML=FALSE)
summary(auto3lmer)

### hdrs_tert = tertiles
auto3lmerT<-lmer(ang_dev ~ angstig_dl*factor(hdrs_tert) + (-1+angstig_dl|subjno),
                 control=list(msVerbose=TRUE, maxIter=500),data=dat2,na.action=na.exclude, REML=FALSE)
summary(auto3lmerT)
auto3lmerT@fixef[2]+c(0,auto3lmerT@fixef[5:6])

################
### sad      ###
################

### hdrs_change as linear term
auto4lmer<-lmer(som_dev ~ somber_dl*hdrs_change + (-1+somber_dl|subjno),
                control=list(msVerbose=TRUE, maxIter=500),data=dat2,na.action=na.exclude, REML=FALSE)
summary(auto4lmer)

### hdrs_tert = tertiles
auto4lmerT<-lmer(som_dev ~ somber_dl*factor(hdrs_tert) + (-1+somber_dl|subjno),
                 control=list(msVerbose=TRUE, maxIter=500),data=dat2,na.action=na.exclude, REML=FALSE)
summary(auto4lmerT)
auto4lmerT@fixef[2]+c(0,auto4lmerT@fixef[5:6])

############################
### COMMUNITY SAMPLE #######
############################

#####################################################################
### variance and correlation analysis for community sample   #######
#####################################################################

rm(list=ls())

dat <- read.table("reshape_corr_twin.csv", header=TRUE, sep=",")
dat <- dat[order(dat$subjno),]
dat$beep <- rep(sequence(sapply(split(dat$subjno, dat$subjno), length)/4), each=4)

### dep_mean_tert==1
res1 <- lme(affect ~ dum_opg + dum_tev + dum_ang + dum_som - 1,
            random = ~ factor(item) - 1 | subjno,
            weights=varIdent(form = ~ 1 | item),
            correlation = corSymm(form = ~ 1 | subjno/beep),
            data=dat, na.action=na.omit,
            control=list(msVerbose=TRUE, maxIter=500, msMaxIter=500), subset=dep_mean_tert==1)
summary(res1)

### dep_mean_tert==2
res2 <- lme(affect ~ dum_opg + dum_tev + dum_ang + dum_som - 1,
            random = ~ factor(item) - 1 | subjno,
            weights=varIdent(form = ~ 1 | item),
            correlation = corSymm(form = ~ 1 | subjno/beep),
            data=dat, na.action=na.omit,
            control=list(msVerbose=TRUE, maxIter=500, msMaxIter=500), subset=dep_mean_tert==2)
summary(res2)

### dep_mean_tert==3
res3 <- lme(affect ~ dum_opg + dum_tev + dum_ang + dum_som - 1,
            random = ~ factor(item) - 1 | subjno,
            weights=varIdent(form = ~ 1 | item),
            correlation = corSymm(form = ~ 1 | subjno/beep),
            data=dat, na.action=na.omit,
            control=list(msVerbose=TRUE, maxIter=500, msMaxIter=500), subset=dep_mean_tert==3)
summary(res3)

#########################################################
### autocorrelation analysis for community sample   #######
#########################################################

rm(list=ls())
dat2 <- read.table("data_twins.csv", header=TRUE, sep=",") #this may take some time
```

```
dat2 <- read.table("data_twins.csv", header=TRUE, sep=",") #this may take some time

################
### cheerful ###
################

### dep_fut as linear term
auto1lmer<-lmer(opgewkt_d ~ opgewkt_dl*dep_fut + dep1 + (-1+opgewkt_dl|subjno),
                control=list(msVerbose=TRUE, maxIter=500),data=dat2,na.action=na.exclude, REML=FALSE)
summary(auto1lmer) # check interaction effect

### dep_mean_tert = tertiles
auto1lmerT<-lmer(opgewkt_d ~ opgewkt_dl*factor(dep_mean_tert) + dep1+ (-1+opgewkt_dl|subjno),
                 control=list(msVerbose=TRUE, maxIter=500),data=dat2,na.action=na.exclude, REML=FALSE)
summary(auto1lmerT)
auto1lmerT@fixef[2]+c(0,auto1lmerT@fixef[6:7])

################
### content  ###
################

### dep_fut as linear term
auto2lmer<-lmer(tevreden_d ~ tevre_dl*dep_fut + dep1 + (-1+tevre_dl|subjno),
                control=list(msVerbose=TRUE, maxIter=500),data=dat2,na.action=na.exclude, REML=FALSE)
summary(auto2lmer)

### dep_mean_tert  = tertiles
auto2lmerT<-lmer(tevreden_d ~ tevre_dl*factor(dep_mean_tert)+ dep1 + (-1+tevre_dl|subjno),
                 control=list(msVerbose=TRUE, maxIter=500),data=dat2,na.action=na.exclude, REML=FALSE)
summary(auto2lmerT)
auto2lmerT@fixef[2]+c(0,auto2lmerT@fixef[6:7])

################
### anxious  ###
################

### dep_fut as linear term
auto3lmer<-lmer(angstig_d ~ angstig_dl*dep_fut+ dep1 + (-1+angstig_dl|subjno),
                control=list(msVerbose=TRUE, maxIter=500),data=dat2,na.action=na.exclude, REML=FALSE)
summary(auto3lmer)

### dep_mean_tert = tertiles
auto3lmerT<-lmer(angstig_d ~ angstig_dl*factor(dep_mean_tert)+ dep1 + (-1+angstig_dl|subjno),
                 control=list(msVerbose=TRUE, maxIter=500),data=dat2,na.action=na.exclude, REML=FALSE)
summary(auto3lmerT)
auto3lmerT@fixef[2]+c(0,auto3lmerT@fixef[6:7])

################
### sad      ###
################

### dep_fut as linear term
auto4lmer<-lmer(somber_d ~ somber_dl*dep_fut+ dep1 + (-1+somber_dl|subjno),
                control=list(msVerbose=TRUE, maxIter=500),data=dat2,na.action=na.exclude, REML=FALSE)
summary(auto4lmer)

### dep_mean_tert = tertiles
auto4lmerT<-lmer(somber_d ~ somber_dl*factor(dep_mean_tert)+ dep1 + (-1+somber_dl|subjno),
                 control=list(msVerbose=TRUE, maxIter=500),data=dat2,na.action=na.exclude, REML=FALSE)
summary(auto4lmerT)
auto4lmerT@fixef[2]+c(0,auto4lmerT@fixef[6:7])

######################
### Wald tests #######
######################

rm(list=ls())

### select either results_dep.txt or results_gen.txt for patient or community sample
dat <- read.table("results_dep.txt", header=TRUE, as.is=TRUE)
#dat <- read.table("results_gen.txt", header=TRUE, as.is=TRUE)

vars <- unique(dat$var)

X2 <- rep(NA, length(vars))
b1 <- rep(NA, length(vars))
b2 <- rep(NA, length(vars))
b3 <- rep(NA, length(vars))

z12 <- rep(NA, length(vars))
z13 <- rep(NA, length(vars))
z23 <- rep(NA, length(vars))

for (i in 1:length(vars)) {

   dat.sub <- dat[dat$var == vars[i],]

   b  <- cbind(dat.sub$bi)
```

```
   se <- c(dat.sub$sei)
   V  <- diag(se^2)

   x1 <- c(1, -1,  0)
   x2 <- c(0,  1, -1)
   X  <- rbind(x1, x2)

   X2[i] <- t(X %*% b) %*% solve(X%*%V%*%t(X)) %*% (X %*% b)

   b1[i] <- b[1]; b2[i] <- b[2]; b3[i] <- b[3]

   X <- rbind(c(1, -1,  0))
   z12[i] <- sqrt(t(X %*% b) %*% solve(X%*%V%*%t(X)) %*% (X %*% b))

   X <- rbind(c(1,  0, -1))
   z13[i] <- sqrt(t(X %*% b) %*% solve(X%*%V%*%t(X)) %*% (X %*% b))

   X <- rbind(c(0,  1, -1))
   z23[i] <- sqrt(t(X %*% b) %*% solve(X%*%V%*%t(X)) %*% (X %*% b))

}

pvalX2  <- pchisq(X2, df=2, lower.tail=FALSE)
pvalz12 <- 2*pnorm(z12, lower.tail=FALSE)
pvalz13 <- 2*pnorm(z13, lower.tail=FALSE)
pvalz23 <- 2*pnorm(z23, lower.tail=FALSE)

res <- data.frame(grp1=formatC(b1, digits=2, format="f"),
                  grp2=formatC(b2, digits=2, format="f"),
                  grp3=formatC(b3, digits=2, format="f"),
                  X2=formatC(X2, digits=2, format="f"), df=2, pval=formatC(pvalX2, digits=3, format="f"),
                  z1vs2=formatC(z12, digits=2, format="f"), pval=formatC(pvalz12, digits=3, format="f"),
                  z1vs3=formatC(z13, digits=2, format="f"), pval=formatC(pvalz13, digits=3, format="f"),
                  z2vs3=formatC(z23, digits=2, format="f"), pval=formatC(pvalz23, digits=3, format="f"))
row.names(res) <- vars
print(res)
```